DETECTING FAULTS IN THE PERIPHERAL CIRCUITS AND AN EVALUATION OF SRAM TESTS

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Abstract:

Very little has been published on faults in the memory peripheral circuits, denoted as 'PFs'. This paper shows that PFs will be detected by march tests, provided that they satisfy particular properties, expressed in terms of properties of the algorithm, and of properties of the algorithm stress. The latter consists of the used data backgrounds and addressing directions. The detection capabilities of a set of well-know march algorithms will be established for the PFs. In addition, industrial results from applying this set of tests to a large number of 0.13 micron 512 Kbyte SRAM chips, combined with a variety of stress conditions, will be presented.

Keywords: March tests, data-backgrounds, address directions, fault coverage, peripheral circuit faults.

1 Introduction

With increasing memory densities and clock speeds, the potential for faults in the peripheral circuits, referred to as PFs, is on the rise. This is due to the increased sensitivity to open defects (aggravated by the use of copper wiring) and to capacitive coupling [1, 2, 3]; while the circuits are more time-critical.

Very little has been published on fault models and algorithms for PFs [4]. Much has been published on fault models and algorithms for detecting faults in the address decoders, denoted as AFs, and in the memory cell array, denoted as MFs [5, 6, 7, 8, 9, 10, 11, 12]. The question to be answered is: How capable are the latter algorithms for detecting faults in commercial SRAMs, and for detecting PFs?

This paper establishes fault models for peripheral memory circuits and derives a set of easy to use criteria march tests have to satisfy in order to detect PFs; similar to the detection criteria used for AFs. The newly established criteria will be applied to a set of well-known march tests to show that the statement [8, 10] "all faults in the peripheral circuits are covered with tests for memory cell array faults"

is not (always) correct.

Several papers have been published on the industrial evaluation of tests applied to DRAMs and SRAMs [13, 14, 15, 16]; however, the tests used in those experiments were of that generation. This paper presents the results of applying a large set of modern tests to a large number of SRAM chips, using many different stresses, such as supply voltages, data backgrounds, etc. The results show that the high voltage and high speed stresses are most effective; while March G and March SL have the highest fault coverage, followed by the very time-efficient tests March U and March LR. The Scan test has the property that it detects faults which are very different from the other tests.

The paper is organized as follows: Section 2 describes the notation for march tests and the stresses of interest to this work. Section 3 gives a classification of the traditional memory faults. Section 4 presents the new peripheral circuit faults, together with requirements march tests have to satisfy in order to detect those faults. Section 5 analyzes a set of well-known march tests, including several recently published tests, for their capability of detecting faults in the peripheral circuits, and shows the results of their application to a large number of SRAM chips. Section 6 gives the conclusions.

2 Memory test algorithms and stresses

A test consists of a Base Test 'BT', applied using a particular Stress Combination 'SC'. A BT is a test algorithm, such as, e.g., MATS+ [5]. An SC consists of a combination of values for the different stresses; e.g., $V_{DD}=1.8V, Temp=70^{0}C$, etc.

Because most BTs have a march test format, below the notation of march tests will be given, followed by a description of the stresses of interest to this paper.

2.1 Notation of march tests

A march test is a sequence of march elements. A march element (ME) consists of a sequence of operations applied to every cell (n) is the number of cells in the memory), in either one of two Address Orders 'AOs': Increasing (\uparrow) AO, from cell 0 to cell n-1, or a Decreasing (\downarrow) AO, from cell n-1 to cell 0. When the AO is irrelevant the symbol ' \uparrow ' is used

Example: $\{ \mathfrak{T}(w0); \mathfrak{f}(r0, w1); \Downarrow (r1, w0) \}$ is the MATS+ test [5]. It consists of three march elements: M0, M1 and M2. M1: $\mathfrak{f}(r0, w1)$ means 'for i = 0 to n - 1 do {read A[i] with expected value 0; A[i] := 1}'.

2.2 Stresses combinations

When testing, each BT is applied using several *stresses*. The stresses can be divided into algorithm stresses and non-algorithm stresses.

A non-algorithm stress, also referred to as an environmental stress, specifies the environmental values, such as the supply voltage, the temperature, the timing (the clock frequency), etc.; they are effective during the application of the test.

An algorithm stress specifies the way the test is performed, and therefore it influences the sequence and/or the type of the memory operations. The most known algorithm stresses are the address direction and data-background.

Address Direction 'AD' is the addressing extension of the one-dimensional address order 'AO' to the two dimensional space of the memory cell array. A real memory consists of a number or rows and columns (and thus also of a number of diagonals). The AD specifies the direction (i.e., rows, columns, or diagonals) in which the address sequence has to be performed. The commonly used ADs in the industry are described below.

- Fast X (fX): With fX addressing, each address increment or decrement operation causes an adjacent physical row to be accessed.
- Fast Y (fY): With fY addressing, each address increment or decrement operation causes an adjacent physical column to be accessed.
- Fast D (fD): With fD addressing, each address increment or decrement operation causes an adjacent physical diagonal to be accessed. Fast D is used less frequently in industry.

Data Background 'DB' is the pattern of ones and zeros as seen in an array of memory cells. The most common types of DBs are:

Solid (sDB): all 0s (i.e., 0000.../0000...) or all 1s

Table 1. Single and two-cell faults

| Single-cell faults | | Two-cell faults | | | | | | | |
|-------------------------|------|----------------------|------|--|--|--|--|--|--|
| Name | FFM | Name | FFM | | | | | | |
| State Fault | SF | State CF | CFst | | | | | | |
| Transition Fault | TF | Transition CF | CFtr | | | | | | |
| Write Destructive Fault | WDF | Write Destructive CF | CFwd | | | | | | |
| Read Destructive Fault | RDF | Read Destructive CF | CFrd | | | | | | |
| Deceptive RDF | DRDF | Deceptive CFrd | CFdr | | | | | | |
| Incorrect Read Fault | IRF | Incorrect Read CF | CFir | | | | | | |
| | | Disturb CF | CFds | | | | | | |

Checkerboard (bDB): 0101.../1010.../0101.../1010... Column Stripe (cDB): 0101.../0101.../0101.../0101... Row Stripe (rDB): 0000.../1111.../0000.../1111...

3 Classification of memory faults

Faults in memory systems are divided into Memory cell array Faults 'MFs', Address decoder Faults 'AFs' and Peripheral circuit Faults 'PFs'; the latter consist of faults in the write drivers, precharge circuits, sense amplifies, etc. The first two classes of faults are traditional; they have been included for completeness.

3.1 Memory cell array Faults 'MFs'

Memory cell array faults can be divided into single-cell faults and two-cell (i.e., coupling) faults [10, 12, 17, 24].

Single-cell faults: Single-cell faults are faults involving a single cell; i.e., the cell used to sensitize the fault is the same as where the fault appears. *Functional Fault Models (FFMs)*, such as the Transition Fault (TF) and the Read Destructive Fault (RDF), belong to this class of faults. Table 1, left part, shows the single-cell FFMs.

Coupling faults: Coupling Faults (CFs) are faults involving two cells. The state of, or an operation applied to, one cell (called the aggressor cell), influences the state of, or the operation applied to, the victim cell. Table 1, right part, shows the two-cell FFMs.

3.2 Address decoder Faults 'AFs'

The traditional Address decoder Faults 'AFs' [10] are described below, together with their detection condition.

Traditional AFs: The following types of AFs have traditionally been the faults considered to occur in address decoders:

- AFna: An address does not access its cell.
- AFmc: An address uniquely accesses multiple cells;
 i.e., this is the only address accessing those cells.

- AFma: A cell is uniquely accessed by multiple addresses; i.e., these addresses *only* access that cell.
- · AFoc: An address additionally accesses other cells.

Detection condition for traditional AFs: Any march test will detect AFna through AFoc if it satisfies *Condition AF* for $h \ge 1$ [10, 18]. It consists of the following two march elements (Note: the suffix 'u' denotes up for the \uparrow AO, the suffix 'd' denotes down for the \Downarrow AO; '...' means any number of read (r) or write (w) operations, \overline{x} means NOT x, and $[, r\overline{x}]^h$ $([, rx]^h)$ means h (from hammer) $r\overline{x}$ (rx) operations; $h \ge 0$):

AFh-u: $\uparrow(rx,...,w\overline{x}[,r\overline{x}]^h); x \in \{0,1\}$ **AFh-d:** $\downarrow(r\overline{x},...,wx[,rx]^h); x \in \{0,1\}$

4 Peripheral circuit Faults 'PFs'

Naturally, the peripheral circuits of a memory also can be faulty. The faulty behavior will manifest itself as a speed related fault, or as a fault due to excessive leakage. Speed related faults can occur in the write drivers, the sense amplifiers, and in the precharge circuits; the leakage related fault is due to leaky pass transistors [10, 19].

Below, the reason for the faulty behavior of each peripheral circuit type is given, together with the requirement for detecting that faulty behavior. However, the properties of such requirements will be discussed first.

4.1 Detection requirement properties

The requirements for detecting faults in the peripheral circuits will be expressed in two aspects:

- A. March element properties, and
- B. Algorithm stresses.

A. March element properties

March element (ME) properties consist of the required ME type, and the required Read-Write Sequence 'RWS'. The MEs have two orthogonal properties; see Table 2 (in the table O denotes any operation, $O \in \{r, w\}$):

1. Type: The type of a ME, denoted as the 'MEt', can be marching (denoted as 'MEma') or walking (denoted as 'MEwa').

A ME of type MEmax has the property that before the application of an MEmax the cell is in state \overline{x} , and upon completion of the application of the MEmax the cell is in state x.

A ME of type MEwax has the property that before the application of an MEwax the cell is in state \bar{x} , and upon completion of the application of the MEwax the cell is

Table 2. Taxonomy of March Elements 'MEs'

| ĺ | RWS | ME type | $x; x \in \{0, 1\}$ |
|---|-----|-----------------------------------|---|
| | | MEmax | MEwax |
| | RaW | $1(r\overline{x},,wx)$ | $\uparrow (r\overline{x},,Ox,,w\overline{x})$ |
| | RaR | $1 (r\overline{x},,wx,rx)$ | $1(r\overline{x},,Ox,,r\overline{x})$ |
| | WaW | $\updownarrow(w\overline{x},,wx)$ | $\bigcirc (w\overline{x},,Ox,,w\overline{x})$ |
| | WaR | $1(w\overline{x},,wx,rx)$ | $ \ \ (w\overline{x},,Ox,,r\overline{x}) $ |

again in state \overline{x} ; however, during the application of the MEwax the cell has been changed to in state x.

2. **Read Write Sequence 'RWS':** The RWS is defined by the last operation applied to a given address, together with the first operation applied to the next address.

Examples: the ME ' \uparrow (r0, w1, r1, w1)' applies 4 operations to each cell; the last operation to a cell is the w1 operation, which is followed by a r0 operation applied to the next cell; therefore this is a ME of type MEma1, which applies the Read-after-Write 'RaW' RWS.

The MEmax ' \uparrow ($r\bar{x},...,wx,rx$)', see Table 2, performs the *Read-after-Read* 'RaR' RWS.

The ME ' \uparrow (r0, w1, w0)' is of type MEwa1, and applies a RaW RWS. It has the property that during the application of the MEwa1 to a 4-bit memory, a '1' walks through the memory, as follows: {0000=initial state, 1000=during the application of the ME to cell-0, 0100=during the application of the ME to cell-1, 0010, 0001, 0000=final state}.

B. Algorithm stresses

Algorithm stresses consist of the required address direction 'AD' (e.g., fX or fY) and the used data background 'DB' (e.g., sDB or cDB).

4.2 PFs and their detection conditions

The PFs consist of the following fault models:

- 1. Slow Write Driver Fault (SWDF).
- 2. Slow Sense Amplifier Fault (SSAF).
- 3. Slow PRecharge circuit Fault (SPRF) [4].
- 4. Bit Line Imbalance Fault (BLIF) [10, 19].

Below, the above PFs will be discussed in detail, together with their detection conditions. Table 3 summarizes the march element requirements for detecting each of the above faults; e.g., to detect 'SSAF' fault, a test has to perform a RaW MEmax or a RaW MEwax.

Table 4 shows the most efficient test for each of the PFs, together with the properties of that test; the *Test Length 'TL'*,

which is the total number of read and write operations required for performing the test, varies from 4n for March WDm (for the test for SWDF) to 8n for March WDw and March BLI (for BLIF). The SWDF, the SSAF and the SPRF are detectable by two efficient tests; one based on MEma (therefore e.g., the name of the test 'March SAm' has the suffix m), and another based on the use of MEwa, the name of that test has the suffix w.

Table 3. ME requirements for detecting PFs

| ME p | roperties | | Periphera | l circuit fa | ult | | | | | | | | |
|---------|---|------|-----------|--------------|------|--|--|--|--|--|--|--|--|
| RWS | MEt | SWDF | SSAF | SPRF | BLIF | | | | | | | | |
| RaW | MEmax | l - | + | + | - | | | | | | | | |
| RaR | MEmax | l - | - | - | - | | | | | | | | |
| WaW | MEmax | + | - | - | - | | | | | | | | |
| WaR | MEmax | - | - | - | - | | | | | | | | |
| RaW | MEwax | - | + | + | | | | | | | | | |
| RaR | MEwax | - | - | - | - | | | | | | | | |
| WaW | MEwax | + | - | - | + | | | | | | | | |
| WaR | MEwax | - | - | - | - | | | | | | | | |
| Note: 1 | Note: The RWSs have to be applied using Fast-X addressing, | | | | | | | | | | | | |
| and for | and for both data values, because of asymmetric sensitivities | | | | | | | | | | | | |

SWDF: Slow Write Driver Fault

The Write driver may be too slow due to a defect in the driver circuit and/or due to resistive defects (such as partial open vias) in its path to the to-be-written cells. The result will be that the differential voltage on the bit lines (BLs) during the write operation is reduced. This may cause the cell not to be written. The SWDF will be sensitized by a MEma type ME, using a WaW RWS (see Table 3) with the fX AD and with the bDB or the rDB, see Table 4.

Explanation: the operation 'wx' of the WaW MEma, see Table 2, forces the BLs into one state, while the immediately following ' $w\overline{x}$ ' operation, applied to the next cell in the same column (i.e., to the same BLs), using the fX AD, has to force the BLs into the opposite state. This is the worst stress for the SWDF.

The ME which is the most effective in sensitizing the SWDF is the WaW MEmax ' $\mathfrak{D}(w\overline{x},wx)$ ' (see Table 2), because the two write operations are performed back-to-back; i.e., no other operations in between the wx followed with the $w\overline{x}$ operation occur. A possible 'in between operation' could reduce the effect of the first sensitizing wx operation. The test has to be repeated for x=0 and x=1, because of possible asymmetric sensitivities for the '0' and '1' value of the cell.

Table 4 shows the most efficient test using MEma for the SWDF; in the table, $x \updownarrow$ denotes the AO \updownarrow using fX AD. The MEma $x \updownarrow (wD)$, where D = bDB or D = rDB, writes a sequence of '0, 1, 0, 1, 0, 1, ...' values using fX AD, and therefore equivalent to WaW RWS. The fault is detected with $x \updownarrow (rD)$.

A variation of this test, based on the use of the MEwa, can be designed: it uses WaW MEwa type $\mbox{$\updownarrow$}(wx,w\overline{x},r\overline{x},wx)$ ' (see Table 2), together with the algorithm stresses fX addressing and the sDB or the cDB. The MEwa $\mbox{$\updownarrow$}(wx,w\overline{x},r\overline{x},wx)$ ' can be divided into two MEs $\mbox{$\updownarrow$}(wx)$ and $\mbox{$\updownarrow$}(w\overline{x},r\overline{x},wx)$ without having any impact on the ME type. The resulting test based on WaW MEwa for SWDF is given in Table 4. The first ME in the test $\mbox{$\updownarrow$}(wD)$ ' initializes the columns; the next ME $\mbox{$\iota$}_{x}\mbox{$\updownarrow$}(w\overline{D},r\overline{D},wD)$ ' (where $D\in\{sDB,cDB\}$) performs the required WaW sequences such that the w operations, with opposite data value, are applied back-to-back to sensitize the fault. That fault is detected by the read operation.

Note: The SWDF would also be sensitized by any ME of the form ${}^{\prime}\chi \updownarrow (...,wD,w\overline{D},r\overline{D},...){}^{\prime}$, where $D \in \{bDB,rDB\}$. However, then the sensitization would take place by applying the operation sequence ${}^{\prime}wx,w\overline{x}{}^{\prime}$ to the same cell, such that the delay of the row decoder, due to switching from a cell to the next cell, is not included; this will be a less stressy sensitization.

SSAF: Slow Sense Amplifier Fault

The Sense Amplifier 'SA' may be too slow, or is asymmetric (because of some offset voltage) due to a defect in the SA circuits and/or due to resistive defects in the path from the cell to the SA. This may cause read operations to produce incorrect results. The sensitization and detection of the SSAF requires the application of the MEma, using the RaW RWS, (i.e., the ME ' \uparrow ($r\bar{x},...,wx$)'); for x=0 and x=1, together with the algorithm stresses fX addressing and the sDB or cDB. Hence the MEma $\chi \uparrow$ (rD,wD) and the MEma $\chi \uparrow$ (rD,wD), where $D \in \{sDB,cDB\}$ are required for the detection of SSAF; see Table 4.

E.g., the operation 'w0' brings the BLs in the worst case state for the following 'r1' operation, applied to the next cell in the same column; hence the use of fX addressing and the sDB or the cDB.

A variation of this test, based on the use of the MEwa, can be designed: it uses MEwa type MEs with the RaW RWS, together with the algorithm stresses fX addressing and the bDB or the rDB; see Table 4. The first ME in the test '(wD)' writes the sequence '(0,1,0,1,...)'; the next ME '(xD)' (where $D \in \{bDB, rDB\}$) performs the required RaW sequence such that the r operation and the w operation operate on opposite data values. E.g., a read 1 operation is applied to the next cell c_2 after a write 0 operation is applied to cell c_1 , which is adjacent and belongs to the same column as cell c_2 .

Note: The SPRF would also be sensitized and detected with any ME of the form ' \updownarrow (..., $rx, w\overline{x}, r\overline{x}, ...$)'. However, then the sensitization would take place by applying the operation sequence ' $rx, r\overline{x}$ ' to the same cell, such that the delay

Table 4. Efficient tests for PFs

| [| | | | Test prope | erties | | | | | | | |
|------|--|-------|----|------------|--------|----------|--|--|--|--|--|--|
| # | Name | Fault | TL | MEt | RWS | DB* | Test; $D = DB$ | | | | | |
| 1 | March WDm | SWDF | 4n | MEma | WaW | bDB, rDB | $\{\chi \hat{\mathfrak{J}}(wD); \chi \hat{\mathfrak{J}}(rD); \chi \hat{\mathfrak{J}}(w\overline{D}); \chi \hat{\mathfrak{J}}(r\overline{D})\}$ | | | | | |
| 2 | March WDw | SWDF | 8n | MEwa | WaW | sDB, cDB | $\{ (wD);_X (w\overline{D}, r\overline{D}, wD); (w\overline{D});_X (wD, rD, w\overline{D}) \}$ | | | | | |
| 3 | March SAm | SSAF | 5n | MEma | RaW | sDB, cDB | $\{ (wD);_X (rD, w\overline{D});_X (r\overline{D}, wD) \}$ | | | | | |
| 4 | March SAw | SSAF | 6n | MEwa | RaW | bDB, rDB | $\{ (wD);_X (rD,wD);_X (w\overline{D});_X (r\overline{D},w\overline{D}) \}$ | | | | | |
| 5 | March PRm | SPRF | 5n | MEma | RaW | sDB, cDB | $\{ (wD)_{;X} (rD, w\overline{D})_{;X} (r\overline{D}, wD) \}$ | | | | | |
| 6 | March PRw | SPRF | 5n | MEwa | RaW | bDB, rDB | $\{ \{ (wD);_X \} (rD,wD);_X \} (w\overline{D});_X \} (r\overline{D},w\overline{D}) \}$ | | | | | |
| 7 | March BLI | BLIF | 8n | MEwa | WaW | sDB, cDB | $\{ \mathfrak{J}(wD);_{X} \mathfrak{J}(w\overline{D}, r\overline{D}, wD); \mathfrak{J}(w\overline{D});_{X} \mathfrak{J}(wD, rD, w\overline{D}) \}$ | | | | | |
| *: ' | *: The notation 'bDB, rDB' means the use of bDB or rDB | | | | | | | | | | | |

of the row decoder is not included; this will be a less stressy sensitization.

SPRF: Slow PRecharge circuit Fault

The Prechage Circuit 'PC' may be too slow, or it may not precharge both BLs to the same voltage level, due to defects in the PC circuitry and/or due to resistive defects in the BLs [4]. The result may be that especially read operations will produce incorrect results, because they are most sensitive to BL voltage offset errors.

The sensitization and detection of the SPRF require the application of the MEma ' $\updownarrow(r\overline{x},...,wx)$ '; for x=0 and x=1, together with fX addressing and the sDB or the cDB. Hence the MEma $\chi \uparrow (rD,w\overline{D})$ and the MEma $\chi \uparrow (r\overline{D},wD)$, where $D \in \{sDB,cDB\}$ are required for the detection of SPRF; see Table 4.

A variation of this test, based on the use of the MEwa, can be designed: it uses MEwa type MEs with the RaW RWS, together with the algorithm stresses fX addressing and the bDB or the rDB; see Table 4. The explanation is similar to that given for the detection condition of SSAF. E.g., the operation 'w0' brings the BLs in the worst case state for the following 'r1' operation, applied to the next cell in the same column:

Note: This fault would also be sensitized and detected with any ME of the form ' \updownarrow (...,rx, $w\overline{x}$, $r\overline{x}$,...)'. However, then the sensitization would take place by applying the operation sequence 'rx, $r\overline{x}$ ' to the same cell, such that the delay of the row decoder is not included; this will be a less stressy sensitization. Alternatively, the SPRF would be sensitized and detected with a RaR RWS of the form ' \updownarrow ($r\overline{x}$,...,rx)'; however, the stress caused by the 'rx' operation will be much less than that of the 'wx' operation of the RaW RWS.

It is important to note here that the requirements for detecting SPRF are the same as those required for detecting SSAF. Therefore they can be detected using the same tests; see Table 4, where one can clearly see that March SAm is the same as March PRm, and March SAw is the same as March PRw.

BLIF: Bit Line Imbalance Fault

With decreasing feature widths, the transistors increasingly draw more current in the off-state. This also applies to the pass transistors, which may impact the possibility of reading the correct value of a cell (write operations are less sensitive). The worst case situation occurs when a 'rx' operation is applied to a cell, which is the only cell in that column containing the value 'x'. Then, while reading the cell with the 'x' value, the leaky pass transistors of the cells with the \overline{x} value will neutralize the read result, to the extent that the incorrect ' \overline{x} ' value may be read. The sensitization and detection of the BLIF requires the application of the WaW MEwa ' $(wx, w\overline{x}, r\overline{x}, wx)$ ' (see Table 2); for x = 0 and x = 1, together with fX addressing and the sDB or the cDB. The MEwa ' $(wx, w\overline{x}, r\overline{x}, wx)$ ' can be divided into two MEs $\mathfrak{I}(wx)$ and $\mathfrak{I}(w\overline{x}, r\overline{x}, wx)$ without impacting the MEwa type. The resulting test for BLIF based on WaW MEw is given in Table 4.

Explanation: e.g., the MEwa operation 'w1' brings a single cell in state '1', after which it is read; while all other cells in the same column contain the value '0'.

Note that the required WaW MEwa for BLIF is the same as that required for SWDF based on MEwa; see Table 4.

Minimal test set for PFs

Based on the above, one can conclude that in order to detect all targeted PFs at least two march tests have to be used:

- March WDw and March SAm, or
- March WDw and March SAw.

Using the first two tests is recommended since they combine a test based on MEwa and a test based on MEma; each test has to be used with differen DB; e.g., one with sDB and one with cDB. From industrial point of view, it has been shown that using different DBs has a large impact on the fault coverage and can detect some non-modeled (non-known) faults [14, 15, 16]. The minimal test set for PFs is given in Table 5; the tests are renamed as March BLI-WDw (for BLIF and SWDF) and March SAPRm and March SAPRw (for SSAF and SPRF).

Table 5. Minimal test set for PFs

| # | Name | TL | DB | Description; D=DB | FC | | | | |
|---|--------------|----|------------|--|------------|--|--|--|--|
| 1 | March BLIWDw | 8n | sBd or cDB | $\{ \widehat{\mathbb{T}}(wD);_{X} \widehat{\mathbb{T}}(w\overline{D}, r\overline{D}, wD); \widehat{\mathbb{T}}(w\overline{D});_{X} \widehat{\mathbb{T}}(wD, rD, w\overline{D}) \}$ | BLIF, SWDF | | | | |
| 2* | March SAPRm | 5n | sDB or cDB | $\{ \widehat{\mathbb{T}}(wD);_{X} \widehat{\mathbb{T}}(rD,w\overline{D});_{X} \widehat{\mathbb{T}}(r\overline{D},wD) \}$ | SSAF, SPRF | | | | |
| 3* | March SAPRw | 6n | bDB or rDB | $\{ \mathfrak{J}(wD);_{X} \mathfrak{J}(rD,wD);_{X} \mathfrak{J}(w\overline{D});_{X} \mathfrak{J}(r\overline{D},w\overline{D}) \}$ | SSAF, SPRF | | | | |
| *: Only test 3 or test 2 has to be used with test 1 | | | | | | | | | |

Table 6. Algorithms used in the experiment

| # | BT | TL | Algorithm, also named BT |
|------|-------------------------|---------|---|
| | Scan [8] | 4n | $\{ \uparrow(w0); \uparrow(r0); \uparrow(w1); \uparrow(r1) \}$ |
| 2 | MATS+ [5] | 5n | $\{ (w0); (r0, w1); \psi(r1, w0) \}$ |
| 3 | MATS++ [10] | 6n | $\{ \mathfrak{J}(w0); \mathfrak{h}(r0,w1); \Downarrow (r1,w0,r0) \}$ |
| 4 | March B [6] | 17n | $\{ \mathfrak{P}(w0); \! \! \! \! \! \! \! \! \! \! \! \! \! \! \! \! \! \! $ |
| 5 | March C- [10] | 10n | $\{\mathring{\updownarrow}(w0); \Uparrow(r0,w1); \Uparrow(r1,w0); \Downarrow(r0,w1); \Downarrow(r1,w0); \mathring{\updownarrow}(r0)\}$ |
| 6 | March G [20] | * | $\{ (w0); \uparrow (r0, w1, r1, w0, r0, w1); \uparrow (r1, w0, w1); \psi (r1, w0, w1, w0); \psi (r0, w1, w0); \psi (r$ |
| | | | $Del; \mathfrak{J}(r0, w1, r1); Del; \mathfrak{J}(r1, w0, r0) \}$ |
| 7 | March LA [21] | 22n | $\{ \mathfrak{J}(w0); \hspace{0.1cm} 0.1cm$ |
| | | | $\Downarrow (r1, w0, w1, w0, r0); \Downarrow (r0)\}$ |
| 8 | March LR [22] | 14n | $ \left\{ \{ (w0); \Downarrow (r0,w1); \Uparrow (r1,w0,r0,w1); \Uparrow (r1,w0); \Uparrow (r0,w1,r1,w0); \Downarrow (r0) \right\} $ |
| 9 | March RAW[23] | 26n | $\{ \{(w0); \uparrow(r0, w0, r0, r0, w1, r1); \uparrow(r1, w1, r1, r1, w0, r0); \downarrow(r0, w0, r0, r0, w1, r1); \}$ |
| | | | $\Downarrow (r1,w1,r1,r1,w0,r0); \updownarrow (r0)\}$ |
| 10 | March SR [12] | 14n | $ \left\{ \Downarrow (w0); \Uparrow (r0,w1,r1,w0); \Uparrow (r0,r0); \Uparrow (w1); \Downarrow (r1,w0,r0,w1); \Downarrow (r1,r1) \right\} $ |
| 11 | March SS [12, 24] | 22n | $\{((w0); ((r0, r0, w0, r0, w1); ((r1, r1, w1, r1, w0);), ((r0, r0, w0, r0, w1); \})\}$ |
| | | | $\Downarrow (r1,r1,w1,r1,w0); \Uparrow (r0)\}$ |
| 12 | March SL [25] | 41n | $\{ (w0); (r0, r0, w1, w1, r1, r1, w0, w0, r0, w1); (r1, r1, w0, w0, r0, r0, w1, w1, r1, w0); \}$ |
| 1 | | | |
| 13 | March U [26] | 13n | $\{ \{ (w0); \uparrow(r0,w1,r1,w0); \uparrow(r0,w1); \ \psi(r1,w0,r0,w1); \ \psi(r1,w0) \}$ |
| 14 | Algorithm B [7] | 17n | $\{ (w0); (r0, w1, w0, w1); (r1, w0, r0, w1); (v1, w0, w1, w0); (v0, w1, r1, w0) \}$ |
| 15 | PMOVI [27, 28, 29] | 13n | $\{ \psi(w0); \Uparrow(r0,w1,r1); \Uparrow(r1,w0,r0); \psi(r0,w1,r1); \psi(r1,w0,r0) \}$ |
| *: T | he TL is $23n + 2Del$; | where D | el is the delay time required for detecting Data Retention Faults |

5 Test evaluation

A set of 39 BTs has been applied to a large set of 0.13 micron 512 Kbyte SRAM chips, using the following stresses:

- Algorithm stresses
 - Addressing: Fast X 'fX' and Fast Y 'fY'.
 - Data-backgrounds: Solid (sDB), Checkerboard (bDB), Column Stripe (cDB), and Row Stripe (rDB).
- Environmental stresses
 - Voltage: high Voltage (+V) and low Voltage (-V)
 - Speed: high Speed (+S) and low Speed (-S)

The consequence is that each BT is applied 2(Voltage) $\times 2(\text{Speed}) \times 2(\text{Addressing}) \times 4(\text{DB})=32 \text{ times}$. Therefore, a total of $39 \times 32 = 1248$ tests have been applied. However, 24 BTs produced results which were not very interesting; therefore, the results of the interesting 15 BTs, which means $15 \times 32 = 480$ tests, will be discussed.

Table 6 shows this set of BTs. The left column shows the number of the BT, the column 'BT' lists the name of the BT; the last column gives the description of the algorithm.

The results of the evaluation are presented in two parts: an analytical evaluation of the capability of the tests of Table 6, in terms of being able to detect Peripheral circuit Faults 'PFs', and an industrial evaluation by applying the tests of Table 6 to a large number of SRAM chips, using the above SCs.

5.1 Analytical analysis

The requirements for detecting PFs, see Table 3 and Table 4, can be applied to the BTs of Table 6; the result is shown in Table 7. The column 'MEt' describes the March Element type of the corresponding BT, as defined in Section 4. Similarly, the column 'RWS' lists the Read-Write Sequence, as specified in the corresponding BT. The columns 'SWDF', 'SSAF', and 'SPRF' list the required algorithm stress for detecting those PFs. Note that the detection of BLIFs requires a test with MEs of type MEwa, using the WaW RWS; see Table 3. None of the tests of Table 7 have that property; therefore the column 'BLIF' is absent in Table 7. Similarly, the column 'AD' is absent, because all PFs require the ' $\chi \uparrow$ ' AD. The required Data Backgrounds 'DBs' are fault specific; they are given under the columns 'SWDF', 'SSAF', and 'SPRF'.

Table 7. Algorithm stress for detecting PFs

| | _ | | | | |
|-----------|------------|----------------|---------|--------------|----------|
| Algorithr | n (BT) and | its properties | Require | ed algorithm | n stress |
| BT | MEt | RWS | SWDF | SSAF | SPRF |
| Scan | ma | WaW,RaR | b,r | - | - |
| MATS+ | ma | RaW | - | s,c | s,c |
| MATS++ | ma | RaW,RaR | - | - | - |
| March B* | wa; ma | RaW | - | s,c; b,r | s,c; b,r |
| March C- | ma | RaW | | s,c | s,c |
| March G* | wa; ma | RaR;RaW | - | s,c; b,r | s,c; b,r |
| March LA | ma | RaR | 'l - | - | - |
| March LR* | wa;ma | RaR; RaW | - | s,c; b,r | s,c; b,r |
| March RAW | ma | RaR | - | - | - |
| March SR | wa;ma | RaW,RaR;WaW | b,r | b,r | b,r |
| March SS | ma | ` RaW | - | s,c | s,c |
| March SL | ma | RaW | - | s,c | s,c |
| March U* | wa;ma | RaW | - | s,c;b,r | s,c;b,r |
| Algor, B* | wa;ma | RaW | - | s,c;b,r | s,c;b,r |
| PMOVI | ma | RaR | - | - | - |

*: The DBs (e.g., for March B) is 's,c' for 'ma' MEt and 'b,r' for 'wa' MEt

's,c' means sDB or cDB; 'b,r' means bDB or rDB

The required AD is 'x ft'; it is the same for all PFs

Note: None of the BTs satisfy the requirements for detecting BLIFs

From Table 7 it can be concluded that the Scan and March SR are the only BTs capable of detecting SWDFs. MATS++, March LA, March RAW and PMOVI cannot detect any PFs; while March B, March G, March LR, March U and Algorithm B can detect SSAFs and SPRFs in more than one way: using MEs of type MEma or of type MEwa. It should be noted that a PF is considered detected by a march test if the test satisfies the MEt with the corresponding RWS together with the algorithm stress for both x=0 and x=1; see Section 4.2.

5.2 Experimental results

The application of the 15 BTs, using 32 SCs, results in 480 tests. These will be discussed in terms of the following subjects:

- Influence of environmental stresses
- · Influence of algorithm stresses

Influence of environmental stresses The influence of the environmental stresses will be analyzed using Table 8. The table consists of four subtables; one for each combination of the values of the Speed (+S and -S) and Voltage (+V and -V) stresses. Each subtable has the following structure: The column '#', as listed in Table 6, shows the BT# of the BT listed in column 'Base Test'. In order to save space, 8 out of the 15 BTs of Table 6 have been selected. The set of 8 BTs consists of 6 BTs with the highest Fault Coverage 'FC'; the other two BTs are Scan and PMOVI. They are selected because of their special properties, as will follow later.

The column 'FC' lists the Fault Coverage (FC) of the corresponding BT, while the column 'UF' lists the number of *Unique Faults* 'UFs' detected with the BT. A UF is a fault which is only detected with a single BT; i.e., none of the other BTs, or tests, in that table do detect that fault. The

columns '1, 4, 6, ..., 15' represent the same BTs as listed in column '#'; they form a matrix of FCs.

The **bold-face** diagonal entries of the matrix list the FC of the corresponding BT; for ease of reference, these entries are also listed in the column 'FC'.

The entries *below* the bold-face diagonal list the FC of the *union* of the FCs of the corresponding two tests. For example, in the +S+V subtable, the FC of March G is 120 and of Scan is 113; the *union* of the FCs is 124 (printed in *italics* in the +S+V subtable); this is the number of faults Scan and March G detect *together*.

The entries *above* the bold-face diagonal list the FC of the *intersection* of the FCs of the corresponding two tests. For example, the *intersection* of the FCs of March G and Scan is 109 (printed in italics in the +S+V subtable); this is the number *common* faults detected with both March G and Scan

Table 10 summarizes the influence of the environmental SCs on the FC of the BTs; the entries have been derived from Table 8. The table shows that the stress +S results in a higher FC than -S, and +V in a higher FC than -V. The SC +S+V has the highest FC, and -S-V the lowest.

Table 10 also shows that different BTs obtain their highest FC with different environmental SCs; e.g., the very simple 13n BT 'March U' has the highest FC for the SCs +S-V and -S-V; which is very interesting. Note that March U, March LR and March SR are BTs which contain MEs of type MEwa, see Table 6 and Table 7; this makes them very different from the more traditional march tests based on MEs of type MEma, such that they also may detect different types of faults. March U and March LR appear 3 out of 6 times in column 'Highest FC', and 3 out of 4 times in column 'Highest Union'; while they do not appear in the column 'Lowest FC'!

Note that Algorithm B [7] has been designed for detecting the same faults as March B [7], except for the fact that it is more symmetric, which facilitates its implementation. March B has been extended to become March G[20], in order to cover data retention faults; see Table 6. Therefore, the potential presence of Data Retention Faults 'DRFs' may explain the high FC of March G.

From Table 8 one can conclude that the BTs Scan and PMOVI have the lowest FC; however, they have been included for other purposes. Scan is the only test capable of detecting SWDFs, such that in many situations it does detect unique faults 'UFs' [14, 15]. MOVI has been included because, although it typically has a lower FC than March C-, which is of the same complexity, it detects speed related faults [10], address decoder delay faults [29], and many unique faults in DRAMs [14, 15]. However, in this experiment, MOVI did not outperform the other BTs.

Table 8 shows that the highest Union values in each of the subtables always includes the Scan test, together with an-

| | | | | | Tabl | e 8. | Influ | jeno | e of | env | iror | men | tal st | resse | es | | | | | | | |
|-----|-------------|------|---------|---------|--------|--------|-------|------|--------|-------|--------|---------------------------------|--------|-------|-----|-----|-----|-----|-----|-----|-----|----|
| | | | | | | | | | high S | Speed | (+S) ' | Festing | | | | | | | | | | |
| | | high | Voltage | (+V); | Subtal | ole +S | +V | | | | | low Voltage (-V); Subtable +S-V | | | | | | | | | | |
| # | Base Test | FC | UF | 1 | 4 | 6 | 8 | 12 | 13 | 14 | 15 | # | FC | UF | l | 4 | 6 | 8 | 12 | 13 | 14 | 15 |
| 1 | Scan | 113 | 0 | 113 | 108 | 109 | 109 | 111 | 110 | 109 | 109 | 1 | 96 | 1 | 96 | 91 | 91 | 93 | 90 | 93 | 91 | 89 |
| 4 | March B | 116 | 0 | 121 | 116 | 116 | 115 | 116 | 116 | 116 | 110 | 4 | 103 | 0 | 108 | 103 | 101 | 101 | 99 | 101 | 99 | 96 |
| _ 6 | March G | 120 | 1 | 124 | 120 | 120 | 116 | 118 | 118 | 117 | 112 | 6 | 103 | 0 | 108 | 105 | 103 | 102 | 99 | 102 | 99 | 95 |
| 8 | March LR | 117 | 0 | 121 | 118 | 121 | 117 | 116 | 116 | 115 | 111 | 8 | 105 | 0 | 108 | 107 | 106 | 105 | 99 | 104 | 101 | 96 |
| 12 | March SL | 120 | 0 | 122 | 120 | 122 | 121 | 120 | 119 | 117 | 113 | 12 | 100 | 0 | 106 | 104 | 104 | 106 | 100 | 99 | 98 | 94 |
| 13 | March U | 119 | 0 | 122 | 119 | 121 | 120 | 120 | 119 | 117 | 113 | 13 | 106 | 0 | 109 | 108 | 107 | 107 | 107 | 106 | 102 | 95 |
| 14 | Algorithm B | 117 | 0 | 121 | 117 | 120 | 119 | 120 | 119 | 117 | 111 | 14 | 102 | 0 | 107 | 106 | 106 | 106 | 104 | 106 | 102 | 94 |
| 15 | PMOVI | 113 | 0 | 117 | 119 | 121 | 119 | 120 | 119 | 119 | 113 | 15 | 96 | 0 | 103 | 103 | 104 | 105 | 102 | 107 | 104 | 96 |
| | | | | | | | | | low S | Speed | (-S) 7 | esting | | | | | | | | | | |
| | | high | Voltage | : (+V); | Subta | ble -S | +V | | | | | low Voltage (-V); Subtable -S-V | | | | | | | | | | |
| # | Base Test | FC | UF | 1 | 4 | 6 | 8 | 12 | 13 | 14 | 15 | _ # | FC | UF | 1 | 4 | 8 | 12 | 13 | 14 | 15 | 8 |
| 1 | Scan | 97 | 0 | 97 | 94 | 94 | 94 | 94 | 95 | 96 | 94 | 1 | 85 | 0 | 85 | 82 | 82 | 82 | 81 | 81 | 80 | 80 |
| 4 | March B | 100 | Ô | 103 | 100 | 99 | 100 | 99 | 99 | 97 | 96 | 4 | 99 | 0 | 102 | 99 | 96 | 95 | 92 | 97 | 93 | 91 |
| 6 | March G | 99 | 0 | _102 | 100 | 99 | 99 | 99 | 99 | 97 | 96 | 6 | 97 | 0 | 100 | 100 | 97 | 95 | 92 | 95 | 94 | 91 |
| 8 | March LR | 102 | 0 | 105 | 102 | 102 | 102 | 100 | 99 | 98 | 96 | 8 | 97 | 0 | 100 | 101 | 99 | 97 | 93 | 96 | 93 | 92 |
| 12 | March SL | 100 | 0 | 103 | 101 | 100 | 102 | 100 | 99 | 97 | 96 | 12 | 94 | 0 | 98 | 101 | 99 | 98 | 94 | 93 | 91 | 91 |
| 13 | March U | 100 | 0 | 102 | 101 | 100 | 103 | 101 | 100 | 98 | 96 | 13 | 99 | 0 | 103 | 101 | 101 | 100 | 100 | 99 | 93 | 92 |
| 14 | Algorithm B | 100 | 0 | 101 | 103 | 102 | 104 | 103 | 102 | 100 | 96 | 14 | 95 | 0 | 100 | 101 | 98 | 99 | 98 | 101 | 95 | 91 |
| _15 | PMOVI | 96 | 0 | 99 | 100 | 99 | 102 | 100 | 100 | 100 | 96 | 15 | 92 | 0 | 97 | 100 | 98 | 97 | 95 | 99 | 96 | 92 |

| | # Design For | | | | | | | | | | | | | | | | | |
|----|--------------------|-----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| # | Algorithm | FC | ÜF | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 1 | Scan | 113 | 0 | 113 | 110 | 109 | 108 | 110 | 109 | 109 | 109 | 109 | 110 | 111 | 111 | 110 | 109 | 109 |
| 2 | MATS+ | 115 | 0 | 118 | 115 | 113 | 111 | 114 | 112 | 111 | 112 | 111 | 110 | 113 | 113 | 113 | 112 | 111 |
| 3 | MATS++ | 115 | 0 | 119 | 117 | 115 | 112 | 114 | 113 | 113 | 114 | 113 | 112 | 114 | 113 | 113 | 112 | 111 |
| 4 | March B | 116 | 0 | 121 | 120 | 119 | 116 | 112 | 116 | 113 | 115 | 112 | 113 | 113 | 116 | 116 | 116 | 110 |
| 5 | March C- | 116 | 0 | 119 | 117 | 117 | 120 | 116 | 114 | 113 | 114 | 113 | 112 | 115 | 114 | 114 | 113 | 112 |
| 6 | March G | 120 | 1 | 124 | 123 | 122 | 120 | 122 | 120 | 114 | 116 | 113 | 114 | 114 | 118 | 118 | 117 | 112 |
| 7 | March LA | 115 | 0 | 119 | 119 | 117 | 118 | 118 | 121 | 115 | 115 | 114 | 113 | 114 | 114 | 114 | 113 | 111 |
| 8 | March LR | 117 | 0 | 121 | 120 | 118 | 118 | 119 | 121 | 117 | 117 | 114 | 114 | 115 | 116 | 116 | 115 | 111 |
| 9 | March RAW | 114 | 0 | 118 | 118 | 116 | 118 | 117 | 121 | 115 | 117 | 114 | 112 | 114 | 113 | 113 | 112 | 111 |
| 10 | March SR | 116 | 0 | 119 | 121 | 119 | 119 | 120 | 122 | 118 | 119 | 118 | 116 | 114 | 115 | 114 | 113 | 109 |
| 11 | March SS | 118 | 0 | 120 | 120 | 119 | 121 | 119 | 124 | 119 | 120 | 118 | 120 | 118 | 115 | 114 | 113 | 111 |
| 12 | March SL | 120 | 0 | 122 | 122 | 122 | 120 | 122 | 122 | 121 | 121 | 121 | 121 | 123 | 120 | 119 | 117 | 113 |
| 13 | March U | 119 | 0 | 122 | 121 | 121 | 119 | 121 | 121 | 120 | 120 | 120 | 121 | 123 | 120 | 119 | 117 | 113 |
| 14 | Algorithm B | 117 | 0 | 121 | 120 | 120 | 117 | 120 | 120 | 119 | 119 | 119 | 120 | 122 | 120 | 119 | 117 | 111 |
| 15 | PMOV1 | 113 | 0 | 117 | 117 | 117 | 119 | 117 | 121 | 117 | 119 | 116 | 120 | 120 | 120 | 119 | 119 | 113 |

other BT; this is summarized in the column 'Highest Union' of Table 10. This means that the Scan BT detects more of another class of faults than any of the other BTs. In three of the four cases, the second test is March U or March LR; both contain MEs of type MEwa. Note that the March G (for SC=+S+V) and Scan (for SC=+S-V) detect unique faults 'UFs'.

Tables 8 and 10 show that BTs performed with the environmental SC +S+V have the highest FC. Therefore the subtable +S+V of Table 8 has been extended to include all of the 15 selected tests; see Table 9. This table shows that the FCs of the 15 BTs are very close.

Table 10. Summary of environmental SCs

| SC | | lighest I [*] C | L | west FC | Hig | hest Union | | | | | | |
|--|-----|--------------------------|-----|----------|-----|------------|--|--|--|--|--|--|
| | FC | BTs* | FC | BTs | FC | BTs** | | | | | | |
| +S+V | 120 | March G, SL | 116 | March B | 124 | March G | | | | | | |
| +S-V | 106 | March U | 102 | Alg. B | 109 | March U | | | | | | |
| -S+V | 102 | March LR | 99 | March G | 105 | March LR | | | | | | |
| -S-V | 99 | March B, U | 84 | March SL | 103 | March U | | | | | | |
| *: The notation 'March B, U' means 'March B and March U' | | | | | | | | | | | | |
| **: The highest union always includes Scan as one of the two BTs | | | | | | | | | | | | |

Influence of algorithm stresses

The consequences of the algorithm stresses (AD=fX or fY, and DB=sDB, bDB, rDB or cDB) for the environmental SC +S+V is shown in Table 11. The table consists of 6 subta-

Table 11. Algorithm stresses

| | High Speed (+S) and High V | | | | | | | | | | | | | g(+V) | | | | | | | | |
|-----|----------------------------|-----|----|-----|--------|-----|-----|-----|-----|-----|-----|----------|-----|-------|-----|-----|--------|-----|------|-----|-----|--------|
| | | | | | Scan | | | | | | | | | | | Ma | irch G | | | | | \neg |
| # | SC | FC | UF | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | # | IC. | ÜF | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| ì | fX-sDB | 79 | 0 | 79 | 72 | 72 | 70 | 75 | 71 | 73 | 69 | 1. | 104 | 0 | 104 | 100 | 98 | 102 | 102 | 99 | 101 | 102 |
| 2 | fX-bDB | 89 | 0 | 96 | 89 | 76 | 81 | 74 | 84 | 75 | 82 | 2 | 101 | 0 | 105 | 101 | 97 | 100 | 100 | 98 | 99 | 100 |
| 3 | fX-rDB | 82 | 0 | 89 | 95 | 82 | 76 | 74 | 77 | 75 | 76 | 3 . | 101 | 1 | 107 | 105 | 101 | 98 | 99 - | 96 | 98 | 99 |
| 4 | fX-cDB | 89 | 1 | 98 | 97 | 95 | 89 | 73 | 81 | 73 | 82 | 4 | 105 | 0 | 107 | 106 | 108 | 105 | 103 | 100 | 102 | 103 |
| 5 | fY-sDB | 83 | 0 | 87 | 98 | 91 | 99 | 83 | 76 | 78 | 75 | 5 | 109 | 0 | 111 | 110 | 111 | 111 | 109 | 106 | 108 | 109 |
| 6 | fY-bDB | 92 | 0 | 100 | 97 | 97 | 100 | 99 | 92 | 76 | 85 | 6. | 106 | 0 | 111 | 109 | 111 | 111 | 109 | 106 | 106 | 106 |
| 7 | fY-rDB | 82 | 1 | 88 | 96 | 89 | 98 | 87 | 98 | 82 | 76 | 7 | 108 | 0 | 111 | 110 | 111 | 111 | 109 | 108 | 108 | 108 |
| 8 | fY-cDB | 92 | 0 | 102 | 99 | 98 | 99 | 100 | 99 | 98 | 92 | 8 | 109 | 0 | 111 | 110 | 111 | 111 | 109 | 109 | 109 | 109 |
| Ī | March LR | | | | | | | | | | | March SL | | | | | | 一 | | | | |
| # | SC | FC | UF | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | # | FC | UF | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| 1 | fX-sDB | 102 | 0 | 102 | 100 | 96 | 100 | 100 | 98 | 98 | 100 | 1 | 101 | 0 | 101 | 97 | 95 | 94 | 96 | 94 | 98 | 92 |
| 2 | fX-bDB | 103 | 0 | 105 | 103 | 96 | 99 | 100 | 98 | 98 | 100 | 2 | 100 | 0 | 104 | 100 | 96 | 93 | 97 | 97 | 98 | 95 |
| _ 3 | fX-rDB | 97 | 0 | 103 | 104 | 97 | 97 | 97 | 97 | 96 | 97 | 3 | 96 | 0 | 102 | 100 | 96 | 93 | 94 | 95 | 96 | 93 |
| 4 | fX-cDB | 102 | 0 | 104 | 106 | 102 | 102 | 101 | 99 | 98 | 100 | 4 | 97 | 0 | 104 | 104 | 100 | 97 | 93 | 92 | 95 | 91 |
| 5 | fY-sDB | 110 | 0 | 112 | 113 | 110 | 111 | 110 | 108 | 107 | 109 | 5 | 105 | 0 | 110 | 108 | 107 | 109 | 105 | 100 | 102 | 100 |
| 6 | fY-bDB | 108 | 0 | 112 | 113 | 108 | 111 | 110 | 108 | 106 | 108 | 6 | 105 | 1 | 112 | 108 | 106 | 110 | 110 | 105 | 101 | 101 |
| 7 | fY-rDB | 109 | 1 | 113 | 114 | 110 | 113 | 112 | 111 | 109 | 108 | 7 | 107 | 0 | 110 | 109 | 107 | 109 | 110 | 111 | 107 | 100 |
| 8 | fYcDB | 110 | 0 | 112 | 113 | 110 | 112 | 111 | 110 | 110 | 110 | 8 | 102 | 0 | 111 | 107 | 105 | 108 | 107 | 106 | 109 | 102 |
| | | | | М | arch U | | | | | | | | | | | P | NOVI | | | | | |
| # | SC | FC | UF | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | # | FC | HU | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| ŀ | fX-sDB | 99 | 0 | 99 | 97 | 95 | 97 | 96 | 96 | 97 | 96 | 1 | 99 | 0 | 99 | 95 | 94 | 96 | 97 | 94 | 98 | 95 |
| 2 | fX-bDB | 103 | 0 | 105 | 103 | 99 | 100 | 99 | 100 | 101 | 98 | 2 | 99 | 0 | 103 | 99 | 94 | 96 | 97 | 94 | 97 | 96 |
| 3 | fX-rDB | 100 | 0 | 104 | 104 | 100 | 99 | 98 | 97 | 98 | 96 | 3 | 98 | 0 | 103 | 103 | 98 | 95 | 96 | 94 | 95 | 95 |
| 4 | fX-cDB | 103 | 0 | 105 | 106 | 104 | 103 | 98 | 98 | 100 | 98 | 4 | 100 | 1 | 103 | 103 | 103 | 100 | 97 | 94 | 97 | 97 |
| 5 | fY-sDB | 108 | 0 | 111 | 112 | 110 | 113 | 108 | 106 | 106 | 105 | 5 | 105 | 0 | 107 | 107 | 107 | 108 | 105 | 98 | 102 | 100 |
| 6 | fY-bDB | 110 | 1 | 113 | 113 | 113 | 115 | 112 | 110 | 109 | 105 | 6 | 100 | 0 | 105 | 105 | 104 | 106 | 107 | 100 | 99 | 99 |
| 7 | fY-rDB | 112 | 1 | 114 | 114 | 114 | 115 | 114 | 113 | 112 | 106 | 7 | 104 | 0 | 105 | 106 | 107 | 107 | 107 | 105 | 104 | 100 |
| 8 | fY-cDB | 108 | 0 | 111 | 113 | 112 | 113 | 111 | 113 | 114 | 108 | 8 | 102 | 0 | 106 | 105 | 105 | 105 | 107 | 103 | 106 | 102 |

bles, one for each of the selected BTs. Table 12 summarizes the result.

It is interesting to note that the highest FCs are always obtained for the AD=fY, and the lowest for AD=fX; without exception. This denotes that the particular SRAMs being tested are more sensitive to delays in the column decoder, which could indicate that accessing columns is the most timing critical operation.

The fY addressing, together with the cDB or the sDB, are the most effective; while fX addressing, together with rDB, are the least effective.

The 'Highest Union' almost consistently involves a test using the fY AD, and another test using the fX AD; while with the fX AD typically the sDB is used.

6 Conclusions

In this paper the space of faults in the memory peripheral circuits, denoted as 'PFs', has been explored. The space consists of the Slow Write Driver Fault 'SWDF', the Slow Sense Amplifier Fault 'SSAF', the Slow PRecharge circuit Fault 'SPRF', and the Bit Line Imbalance Fault 'BLIF'. Similar to the detection conditions for address decoder faults, it has been shown that PFs can be detected with march tests, provided that they satisfy particular combinations of the following properties: properties of the algorithm

Table 12. Influence of algorithm SCs

| BT | Highest FC | | Lowest FC | | Highest Union | |
|----------|------------|-------|-----------|-------|---------------|-------|
| | FC | SC* | FC | SC* | FC | SC** |
| Scan | 92 | Yb;Yc | 79 | Xs | 102 | Xs+Yc |
| March G | 109 | Ys;Yc | 101 | Xb;Xr | 111 | Many* |
| March LR | 110 | Ys;Yc | 97 | Χг | 113 | Many* |
| March SL | 107 | Yr | 96 | Xr | 112 | Xs+Yb |
| March U | 112 | Υr | 99 | Xs | 115 | Many |
| PMOVI | 105 | Ys | 98 | Xr | 108 | Xc+Ys |

^{*:} The entries 'Pq' represent the SC of the BT

(the 'march element type' and the 'read-write sequence'), together with properties of the algorithm stress (the address direction and the data background).

The above properties have been analyzed for a large set of well-know tests, while these tests also have been applied to a large number of SRAM chips. The results show that:

- Environmental stresses: High voltage is the most stressful, followed by High Speed; while High Voltage and High Speed is the most stressful combination. The least stressful combination is Low Voltage and Low Speed.
- Algorithm stress: Fast Y addressing is the most stress-

^{&#}x27;P' specifi es the AD; $P \in \{X=fX, Y=fY\}$

^{&#}x27;q' specifi es the DB; q \in {s=sDB, b=bDB, r=rDB, c=cDB}

^{&#}x27;Yb;Yc' means that Yb or Yc can be used

^{**:} Many also includes Xs

- ful Addressing Direction 'AD', and the Solid and the Column Stripe Data Backgrounds are the most stressful DBs.
- Algorithm impact: Scan and March SR are the only algorithms capable of detecting SWDFs; March B, March G, March LR, March SR, March U and Algorithm B are the algorithms containing march elements of type Marching and of type Walking; which makes them very effective in detecting SSAFs and SPRFs. None of the evaluated tests is capable of detecting BLIFs.

In addition, a set of new, efficient, march tests for detecting PFs has been designed, with test lengths between 4n and 8n. The analysis done showed that all targeted PFs can be covered with only two march tests with a total test length of at most 14n.

The above results are, of course design and layout dependent. Evaluating the same memory tests with the same stresses, using a different memory implementation may produce different results.

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